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## **Solution**

# CLASS 7 MATHEMATICS WORKSHEET -5 ( UPTO JULY 2023) - LINES AND ANGLES Class 07 - Mathematics

#### Section A

1.

(c)  $150^{\circ}$ 

**Explanation:** Let first angle = x

Second angle = 5x

We know that supplementary angle are 180°

Then, 
$$x + 5x = 180^{\circ}$$

$$6x = 180^{\circ}$$

$$x = 30^{0}$$

Its supplementary  $5x = 5 \times 30^{\circ} = 150^{\circ}$ 

2. (a) supplementary

**Explanation:** When the sum of the measures of two angles is 180°, the angles are called supplementary angles.

$$x - 10^{O} + 190^{O} - x = 180^{O}$$

$$190^{\circ} - 10^{\circ} = 180^{\circ}$$

$$180^{\circ} = 180^{\circ}$$

$$LHS = RHS$$

3.

(d)  $110^{\circ}$ ,  $70^{\circ}$ 

**Explanation:** We know that two angles are supplementary when they add up to 180 degrees.

Here, first angle =  $110^{\circ}$ 

Second angle =  $70^{\circ}$ 

Then,  $110^{\circ} + 70^{\circ} = 180^{\circ}$ 

Thus, these Angles are Supplementary.

4. **(a)** 115<sup>0</sup>

**Explanation:** AB  $\parallel$  CD

$$\angle ABE = 100^{O}$$

$$\angle BED = 15^{O}$$

Extend CD to point F on BF

 $\angle ABF = \angle CFE$  (corresponding angles)

$$\angle$$
CFE =  $100^{\circ}$  =  $\angle$ DFE

In  $\triangle DFE$ 

∠CDE is a exterior angle

$$\angle$$
CDE =  $\angle$ DFE +  $\angle$ FED

$$=100^{0}+15^{0}$$

$$= 115$$

5.

(c)  $70^{\circ}$ 

**Explanation:**  $\therefore$   $\angle$ XEA =  $\angle$ BEF = 110<sup>o</sup> [vertically opposite angles]

$$\therefore \angle BEF + \angle EFD = 180^{\circ}$$
 [co-interior angles]

$$\Rightarrow \angle EFD = 180^{\circ} - 110^{\circ} = 70^{\circ}$$

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6. **(a)** 120<sup>o</sup>

**Explanation:** When the sum of the measures of two angles is 180°, the angles are called supplementary angles.

$$P + Q = 180^{O}$$

$$60^{O} + Q = 180^{O}$$

$$Q = 180^{O} - 60^{O}$$

$$Q = 120^{\circ}$$

7.

**(b)** 
$$50^{\circ}$$
,  $40^{\circ}$ 

**Explanation:** We know that two angles are complementary when they add up to 90 degrees.

Here, first angle =  $50^{\circ}$ 

Second angle =  $40^{\circ}$ 

Then, 
$$50^{\circ} + 40^{\circ} = 90^{\circ}$$

Thus, these Angles are Complementary.

8.

**(b)**  $30^{0}$ 

**Explanation:** Let the angle be  $x^0$ 

$$x = \frac{1}{5} (180 - x)$$

$$5x = 180 - x$$

$$6x = 180^{\circ}$$

$$\chi = \frac{180}{4}$$

$$x = 30^{0}$$

9.

(c) 
$$90^{\circ}$$
,  $90^{\circ}$ 

**Explanation:** When the sum of the measures of two angles is 180°, the angles are called supplementary angles.

10.

(c) 72°

**Explanation:** Let the angles be 3x and 7x.

Since, angles are supplementary

So, 
$$3x + 7x = 180^{\circ} \Rightarrow 10x = 180^{\circ} \Rightarrow x = 18^{\circ}$$

- $\therefore$  Angles are 3  $\times$  18° i.e., 54° and 7  $\times$  18° i.e., 126°
- $\therefore$  Required difference =  $126^{\circ}$   $54^{\circ}$  =  $72^{\circ}$

**Section B** 

11. **(a)** True

**Explanation:** True

12. **(a)** True

**Explanation:** True

13. **(a)** True

**Explanation:** True

- 14. 1. Parallel
- 15. 1. Interior angles
- 16. 1. 180

17.

**(b)** Both A and R are true but R is not the correct explanation of A.

**Explanation:** Parallel lines are lines in a plane that are always the same distance apart. Parallel lines never intersect.

If two parallel lines are intersected by a transversal then the pair of alternate interior angles are equal. So, (A) and (R) are the true statement and (R) is not the reason for (A).

18. (a) Both A and R are true and R is the correct explanation of A.

**Explanation:** If two parallel lines are cut by a transversal, then the alternate interior angles are equal. So, The measure of the alternate angle of  $65^{\circ}$  is  $65^{\circ}$ .

So, (A) and (R) are the true statement and (R) is the reason for (A).

19.

**(b)** Both A and R are true but R is not the correct explanation of A.

**Explanation:** If the sum of the measures of two angles is 90 degrees, the angles are called complementary angles.

An acute angle is a type of angle that measures less than 90° i.e. measure between 0° to 90°. So, two acute angles can be complementary.

So, (A) and (R) are the true statement and (R) is not the reason for (A).

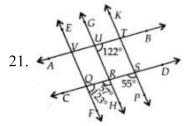
20.

**(b)** Both A and R are true but R is not the correct explanation of A.

**Explanation:** A straight angle is an angle equal to 180 degrees. It is called straight because it appears as a straight line. The sum of angles on a straight line is half of a full turn, which is 180°.

So, (A) and (R) are the true statement and (R) is not the reason for (A).





$$\angle$$
FOR +  $\angle$ ORH =  $123^{\circ}$  +  $57^{\circ}$  =  $180^{\circ}$ 

These angles are on the same side of the transversal CD.

∴ EF || GH

Now, EF || GH and AB is a transversal.

$$\therefore$$
  $\angle$ TUR =  $\angle$ UVQ = 122° [Corresponding angles]

As  $\angle UVQ$  and  $\angle RQF$  are corresponding angles and are not equal.

:. AB and CD are not parallel lines.

22. i.  $\angle 1$  and  $\angle 5$ ,  $\angle 2$  and  $\angle 6$ ,  $\angle 4$  and  $\angle 8$ ,  $\angle 3$  and  $\angle 7$ 

ii.  $\angle 3$  and  $\angle 5$ ,  $\angle 2$  and  $\angle 8$ 

iii.  $\angle 3$  and  $\angle 8$ ,  $\angle 2$  and  $\angle 5$ 

iv.  $\angle 1$  and  $\angle 3$ ,  $\angle 2$  and  $\angle 4$ ,  $\angle 5$  and  $\angle 7$ ,  $\angle 6$  and  $\angle 8$ 

23.  $\angle 4 = \angle 2$  (vertically opposite angles)

$$\angle 4 = 5x, \angle 2 = 91 - 2x$$

$$5x = 91 - 2x$$

$$5x + 2x = 91$$

$$7x = 91$$

$$x = \frac{91}{7}$$

$$x = 13$$

24. Yes,

∠ BOD and ∠ DOA are supplementary because:

Both the angles have common vertex O and a common arm OD

Also,

The non-common arms of both the angles are opposite to each other in direction.

Hence, the angles are supplementary.

25. Since, sum of the measures of the given angles =  $115^{\circ} + 65^{\circ} = 180^{\circ}$ 

Therefore, These angles are supplementary angles.

26. From the above figure, the unknown angles can be obtained as follows:

$$\angle d = 125^{\circ}$$
 (Corresponding angles)

$$\angle e = 180^{\circ} - 125^{\circ} = 55^{\circ}$$
 (Linear pair)

$$\angle f = \angle e = 55^{\circ}$$
 (Vertically opposite angles)

$$\angle c = \angle f = 55^{\circ}$$
 (Corresponding angles)

$$\angle a = \angle e = 55^{\circ}$$
 (Corresponding angles)

$$\angle b = \angle d = 125^{\circ}$$
 (Vertically opposite angles)

# 27. Let the angle be $x^0$

Complement of x is  $(90^{\circ} - x)$ 

Given that the angle is 5 times its complement

$$\Rightarrow$$
 x = 5 (90° - x)

$$\Rightarrow$$
 x =  $450^{\circ} - 5x$ 

$$\Rightarrow 6x = 450^{\circ}$$

$$\Rightarrow x = \frac{450}{6} = 75^{\circ}$$

Hence, the angle which is 5 times to it's complement  $(15^{\circ})$  is  $75^{\circ}$ 

28. From the above figure it can be clearly seen that:

 $\angle$  x is equal to  $100^{\circ}$  as they are corresponding angles

Therefore, 
$$\angle x = 100^{\circ}$$

29. We know that:

Two angles are complementary if sum of their measures is 90°

Here, the pair of angles is 63° and 27°

Sum of the measures of these angles =  $63^{\circ} + 27^{\circ} = 90^{\circ}$ 

As the sum of these angles is equal to  $90^{0}$ 

Therefore, these angles are complementary angles.

30. Let one angle be x and others are y.

Since a transversal intersects two parallel lines, then interior angles on the same side of a transversal are supplementary.

$$x \cdot x + y = 180^{\circ} ...(i)$$

and x - 
$$y = 20^{\circ}$$
 ...(ii) [Given]

Adding (i) and (ii), we get

$$2x = 180^{\circ} + 20^{\circ} = 200^{\circ}$$

$$\Rightarrow x = rac{200^\circ}{2} = 100^\circ$$

Putting value of x in (i), we get

$$100^{\circ} + y = 180$$

$$\Rightarrow$$
 y = 180° - 100° = 80°

Thus, one angle is  $100^{\circ}$  and other is  $80^{\circ}$ 

### **Section D**

# 31. Let first angle be x.

Then its complementary angle is  $90^{\circ}$  – x According to the given problem, we have

$$\frac{x}{90^{\circ}-x} = \frac{7}{11}$$

$$\Rightarrow 11x = 630^{\circ} - 7x$$

$$\Rightarrow 11x + 7x = 630^{\circ}$$

⇒ 
$$18x = 630^{\circ}$$
  
Thus,  $x = 630/18 = 35$   
 $x = 35^{\circ}$ 

Hence, first angle =  $35^{\circ}$ 

and second angle =  $90^{\circ} - x = 90^{\circ} - 35^{\circ} = 55^{\circ}$ 

32. Let required angle be x

Then its supplement =  $180^{\circ}$  – x

According to the given problem, we have

$$x = 180^{\circ} - x - 32^{\circ}$$

$$\Rightarrow x + x = 180^{\circ} - 32^{\circ}$$

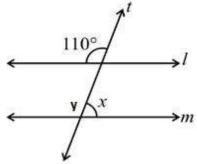
$$\Rightarrow 2x = 148^{\circ}$$

 $\Rightarrow$  x = 148/2 = 74

$$x = 74^{\circ}$$

Hence, the required angle is 74°.

33. From the above figure, we have



$$\angle$$
 y = 110° (Corresponding angles)

Also,

 $\angle x$  and  $\angle y$  form a linear pair of angles. Therefore,

$$\angle x + \angle y = 180^{\circ}$$
 (Linear pair)

$$\angle x + 110^{\circ} = 180^{\circ}$$

$$x = 180^{\circ}$$
 -  $110^{\circ}$ 

$$\angle x = 70^{\circ}$$

Hence, value of  $\angle x$  is  $70^{\circ}$ 

34.  $1 \parallel$  n and q is a transversal.

∴ 
$$6a = 120^{\circ}$$
 [Corresponding angles]  

$$\Rightarrow a = \frac{120^{\circ}}{6} = 20^{\circ}$$

$$\Rightarrow a = \frac{120^{\circ}}{6} = 20^{\circ}$$

Now,  $p \parallel q$  and n is a transversal.

$$\therefore$$
 4c = 120° [Corresponding angles]

$$\Rightarrow c = \frac{120^{\circ}}{4} = 30^{\circ}$$
 ...(i)

Also,  $m \parallel n$  and p are transversal.

 $\therefore$  4c = 3b [Corresponding angles]

$$\Rightarrow$$
 4 × 30<sup>0</sup> = 3b ...[using (i)]  
 $\Rightarrow$  b =  $\frac{120^{\circ}}{3}$  = 40°

Thus,  $a = 20^{\circ}$ ,  $b = 40^{\circ}$  and  $c = 30^{\circ}$ 

- 35. i.  $\angle$ AOD and  $\angle$ DOB;  $\angle$ DOB and  $\angle$ BOC,  $\angle$ BOC, and  $\angle$ AOC;  $\angle$ AOC, and  $\angle$ AOD are four pairs of supplementary angles.
  - ii.  $\angle POS$  and  $\angle SOQ$ ;  $\angle POR$  and  $\angle ROQ$  are two pairs of supplementary angles.
  - iii.  $\angle 1$  and  $\angle 2$ ,  $\angle 3$  and  $\angle 4$ ,  $\angle 5$ , and  $\angle 6$  are three pairs of supplementary angles.

#### **Section E**

$$\therefore$$
  $\angle$ PEB =  $\angle$ EFD [corresponding angles]

$$\Rightarrow 75^{\circ} = 25^{\circ} + y$$

$$\Rightarrow$$
 y = 75° - 25° = 50°

But  $\angle PEB + \angle BEF = 180^{\circ}$  (Linear pair)

$$\therefore 75^{\circ} + 20^{\circ} + \angle 1 = 180^{\circ}$$

$$\Rightarrow \angle 1 + 95^{\circ} = 180^{\circ}$$

$$\Rightarrow \angle 1 = 180^{\circ} - 95^{\circ}$$

$$\Rightarrow \angle 1 = 85^{\circ}$$

In  $\triangle$ EFG,  $\angle$ GEF +  $\angle$ EFG +  $\angle$ EGF = 180° (Sum of angles of a triangle)

$$\Rightarrow \angle 1 + 25^{\circ} + x = 180^{\circ}$$

$$\Rightarrow 85^{\circ} + 25^{\circ} + x = 180^{\circ}$$

$$\Rightarrow 110^{\circ} + x = 180^{\circ}$$

$$\Rightarrow$$
 x = 180° - 110° = 70°

Hence, 
$$x = 70^{\circ}$$
,  $y = 50^{\circ}$ 

37. If one angle = x

Its supplementary angle =  $180^{\circ} - x$ 

$$x = \frac{1}{9}(180^{\circ} - x)$$

$$9x = 180^{\circ} - x$$

$$9x + x = 180^{\circ}$$

$$10x = 180^{\circ}$$

$$x=180^{\circ}/10^{\circ}$$

$$x = 18^{\circ}$$

38. Solution: If  $m \parallel n$  and p and q are transversals

$$\angle 1 = \angle 2 = 123^{\circ}$$
 (alternate interior angles)

$$\angle 3 + \angle 2 = 180^{\circ}$$
 (Linear pair)

$$\angle 3 + 123^{\circ} = 180^{\circ}$$

$$\angle 3 = 180^{\circ} - 123^{\circ} = 57^{\circ}$$

$$\angle 4 + \angle 6 = 180^{\circ}$$

$$85^{\circ} + \angle 6 = 180^{\circ}$$

$$\angle 6 = 180^{\circ} - 85^{\circ}$$

$$\angle 6 = 95^{\circ}$$

 $\angle 5 = 95^{\circ}$ (alternate exterior angles)

$$\angle 2 = 123^{\circ}, \angle 3 = 57^{\circ}, \angle 5 = 95^{\circ}, \angle 6 = 95^{\circ}$$

## **Section F**

## 39. Read the text carefully and answer the questions:

The ratio of angles made by hour hand and second hand to minute hand and second hand is 3:2. Answer the following questions.



- (i) 1. complementary angles
- (ii) (d)  $54^{0}$

Explanation: 54<sup>0</sup>

(iii)(c) 36°

**Explanation:** 36<sup>0</sup>

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(iv)(c) Complementary angles

**Explanation:** Complementary angles

(v) **(b)** False

**Explanation:** False

# 40. Read the text carefully and answer the questions:

Geeta is drawing line with ruler and pencil. The angle made by pencil with a ruler edge is  $50^{\circ}$  as shown below. Find the remaining angles using the concept of parallel lines and transversal.



(i) 1.130

(ii) (d)  $130^{0}$ 

**Explanation:** 130<sup>0</sup>

(iii)(a) 130°

Explanation: 130<sup>o</sup>

(iv)(d)  $50^{0}$ 

**Explanation:** 50<sup>0</sup>

(v) **(a)** True

**Explanation:** True